REVIEW

Reliable change assessment in sport concussion research: a comment on the proposal and reviews of Collie et al

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The proposal of Collie et al for determining reliable change in sports medicine and their review of other current procedures did not address mathematical or theoretical aspects. This article attempts to fill this lacuna, in order to examine the validity of their proposal and the suitability of their review. The conclusions drawn are that Collie et al presented their method too carelessly and their review of other methods leaves serious drawbacks and mistakes unnoticed. A scheme is here provided showing which of the current methods can be used in which situation.

The major aim of the present review is to provide a substantive discussion of the reliable change indices (RCIs) encountered in sports medicine literature, in particular the proposal of Collie et al for the standard error to be used. Since Hinton-Bayre et al advocated the use of the RCI as an objective criterion in sport concussion management, several alternative proposals for the standard error have been presented. All these proposals carry the names SD1 (or SD2), referring, however, to different formulas. The alternative standard errors were chosen without convincing substantive argument, which will leave the clinician in the field confused. The present article attempts to clarify the confusion by discussing their characteristics and underlying assumptions. Secondly, it comments on the review of other current procedures by Collie and colleagues. The fact that I am here personally involved was an extra impetus for writing this review.

APPROACHES TO RELIABLE CHANGE ASSESSMENT IN SPORTS MEDICINE

Several decades ago, McNemar \(^1\) proposed to assess the reliability of change in an individual \(i\) between two measurement moments by considering the observed difference score divided by the standard error of measurement of the difference score: \(D_i/\sigma_{diff}\). When the absolute value of this statistic exceeds 1.96, the null hypothesis of zero true change is rejected and the change was called dependable by McNemar, as the term reliable change was not yet in use. McNemar also provided various formulas for calculation of the standard error under various assumptions within the population of which the person to be assessed is a member. For a general understanding, citing of the basic formula from which all these formulas are derived is inevitable:

\[
\sigma_{diff}^2 = \sigma_X^2 + \sigma_Y^2 - 2\rho_{XY}\sigma_X\sigma_Y
\]

Application of this expression requires knowledge (preferably from external sources) of the standard errors of measurements of the initial testing \(X\) and the final testing \(Y\) of the population variances and the reliability coefficients of \(X\) and \(Y\). The procedure and formulas are based on classical test theory (CTT), and this procedure was christened the classic approach to reliable change assessment. \(^7\) \(^8\)

Hinton-Bayre et al \(^2\) were the first to introduce the reliable change methodology in sport concussion research. They adopted the RCI developed by Jacobson and colleagues, \(^9\) \(^10\) who were the first to use the term. \(^8\) See my recent article \(^1\), for a historical account of the development of the RCI of Jacobson and colleagues, which was eventually established in the psychotherapy literature by Jacobson and Truax \(^1\), and which is, for that reason, also known as the JT index. The JT index comprises a standard error that is in fact equal to the square root of expression 1 adapted to the case where it is assumed that pretest and posttest are parallel—that is, equivalent alternative—measures having equal standard errors of measurement. The RCI of Jacobson et al was meant to be applied in psychotherapy research where it is plausible to assume the absence of confounding effects—for example, practice effects, referring to the phenomenon that individuals who take a test for a second time, or take an alternative form of the test, do better than those who take the test for the first time—thus making the assumption of parallel measures credible. Furthermore, Jacobson and Truax estimated the parameters in expression 1 from the values observed in a control group of healthy people—in particular, the common reliability coefficient of pretest and posttest was estimated by the test-retest reliability. Unfortunately, following Christensen and Mendoza, \(^11\) the denominator was now carelessly named standard error of the difference score and denoted as \(SD\). Thus the formula of the standard error proposed by Jacobson and Truax and adopted by Hinton-Bayre et al became:

\[
SD_{diff} = S_{diff}\sqrt{2} = S_X\sqrt{2(1 - \rho_{XY})}
\]

Abbreviations: CTT, classical test theory; RCI, reliable change index

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Iverson and colleagues adapted expression 1 in a different way. They only assumed that pretest and posttest have a common reliability coefficient, to be estimated by the test-retest reliability observed in a control group of healthy people. The other parameters in expression 1 are estimated by the values observed in this control group as well. Iverson et al. also denoted their standard error as $S_{\text{diff}}$ but for sake of distinction, in the present context I prefer to use $S_{\text{ED}}$. Easy algebra then leads to the following expression for the standard error:

$$S_{\text{ED}} = \sqrt{(S_X^2 + S_Y^2)}(1 - r_{XY}) \quad (3)$$

A third expression for the standard error was recently proposed by Collie et al.:

$$SD_{\text{diff}} = \sqrt{\frac{1}{N-1} \sum \left( D_k - \bar{D} \right)^2} \quad (4)$$

referring to the differences between paired observations observed in a control group of size $N$. Contrary to the preceding standard errors, this expression is not derived from expression 1, but basic statistics textbooks such as that by McNemar demonstrate the following equation:

$$SD_{\text{diff}} = \sqrt{\frac{N}{N-1} \left( S_X^2 + S_Y^2 - 2S_X S_Y r_{XY} \right)} \quad (5)$$

This equation reveals a link between expression 4 and the careless naming (standard error of the difference instead of standard error of measurement of the difference) and the following ambiguous equations presented by Christensen and Mendoza:

$$S_{\text{diff}} = \sqrt{S_X^2 + S_Y^2 - 2S_X S_Y r_{XY}} = \sqrt{2S_{\text{ED}}^2} \quad (6)$$

The left hand equation can be interpreted in two different ways: (a) referring to the stochastic pretest and posttest scores observed in a single person (in which case the expression in the middle should be named standard error of measurement of the difference) or (b) referring to the pretest and posttest scores observed within a sample of people (in which case the expression in the middle is justly named standard error of the difference). Interpretation (a) was clearly the intention of Christensen and Mendoza, as the right hand equation only holds in interpretation (a), under the assumptions of parallel measures and zero effects of testing, and under the null hypothesis of zero true change. Moreover, they described the RCI as a statistic that “represents the amount of difference which one could expect between two scores obtained on the same test by the same individual as a function of measurement error alone” (p 307). However, authors unfamiliar with the classical test theory disregarded interpretation (a) and adhered to the conceptually wrong interpretation (b). Collie et al. cited correctly the formula of the standard error of Jacobson and Truax (although consistently misspelling the latter author’s name). They also are obviously aware of the difference between the concepts of the standard error of the difference and the standard error of measurement of the difference, as they state, probably referring to earlier studies: “The problem with currently applied RC calculations is that the normal amount of variability in change over time within individuals is estimated on the basis of differences between individuals at a single time point! There is no reason to believe that variation between individuals at one time point accurately represents the variation within individuals between two time points.” (p 371). Nevertheless, they propose to calculate the standard error according to expression 4, stating that “this alteration to previous RC calculations produces an RC calculation that is mathematically and theoretically correct”. Thus, after all, Collie et al. followed interpretation (b). Contrary to the classic approach, where an individual’s observed difference is judged by what is regarded exceptional within this individual’s theoretical distribution of measurement errors, Collie et al. judge an individual’s observed difference score by what is designated exceptionally large within the normative sample.

**A THEORETICAL COMPARISON OF THE DIFFERENT APPROACHES**

The RCIs applied in sports medicine are composed of the same numerator—that is, the observed change in a given person—but different standard errors in the denominator. To what extent will the outcomes of these indices differ, and is there a preferred approach?

Expression 3 (the standard error used by Iverson et al.) is clearly preferable to the standard error of the JT index in the case in which the initial and final variance really differ. However, when it is plausible to assume that the variance remains unchanged, the observed initial and final variance may still differ on the basis of chance. The common theoretical value should not be estimated by only the initial variance (as Jacobson and Truax proposed) but by pooling initial and final variance. The outcomes of the JT index and those of the RCI with expression 3 in the denominator will differ to the extent that the final variance differs from the initial variance.

Although it has already been noted that, for conceptual reasons, expression 3 is also preferable to expression 4, it is still worth examining the difference between outcomes of the two approaches. According to CTT, the variance of the differences observed in the control sample can be split into two components: a variance of “true” changes (including effects of testing) and an error variance component:

$$SD_{\text{diff}}^2 = \text{Var}(\Delta + \pi) + S_{\text{ED}}^2 \quad (7)$$

where $\Delta$ denotes the true change and $\pi$ the effect of repeated testing in the members of the control group. For those who are not familiar with CTT, the following analogy may be helpful. Every researcher who applies analysis of variance when comparing group means is familiar with the concept of splitting the total observed variance into the between group variance and the within group variance. This applies to ordinary scores as well as to difference scores. The analogy with analysis of variance reveals when the (conceptual) distribution of possible replications under similar circumstances within a person is regarded as a group of scores, each participant identifying a different group. The group mean is by definition—a basic definition of CTT—the true change (including the non-random test effect) in that person. The variance of the true changes can be regarded as between group variance. The random variance component is the variance of the (conceptually) possible replications within a person. In CTT, these random variance components are assumed to be equal across individuals, and is named error variance of measurement of the difference (thus $S_{\text{ED}}^2$).

Considering the definition of an RCI, for the calculation of the standard error only the random error variance within individuals is needed, whereas Collie et al. also include the between group variance. Under the null hypothesis of zero true change and in the absence of varying...
effects of testing, the between person variance of the differences is zero, and expressions 3 and 4 prove to be equivalent. Expressions 3 and 4 will also be equal when all the participants in the control sample experience the same practice effect. However, when differential practice effects occur, expression 4 is larger than expression 3.

In addition to this theoretical view, I have shown that the standard error according to Collie et al is larger than expression 3, when the initial and final variance observed in the control group differ. The larger the difference between the initial and the final variance and the larger the test-retest reliability, the larger is the difference between the two standard errors.

**HOW TO ACT WHEN INITIAL AND FINAL VARIANCE DIFFER**

Two subsequent assessments of the same test in a control group without intervention and without the occurrence of test effects “ideally” yield equal initial and final group mean, and equal initial and final variance. When these ideal circumstances are met, the distinctive RCIs incorporating expressions 2, 3, or 4 will yield the same outcomes. However, chance has already been mentioned as a cause of differing initial and final variance. Whether a difference between correlated variances can be explained on the basis of chance or not can be tested with a statistic called in from basic text books:

\[ t = \frac{(S_X^2 - S_Y^2)\sqrt{N-2}}{2S_XS_Y\sqrt{1-r_{XY}}} \]  

(8)

which follows a \( t \) distribution with \( df = N-2 \).

Effects of testing are a second possible cause of differing initial and final variance. Therefore the distinction between the standard errors under review is particularly relevant when measures are used that are susceptible to effects of testing. In sports medicine research, as in neuropsychology research, tests measuring cognitive function are typically used, and effects of testing should then be expected, in particular practice or learning effects. When the regression of the final scores on the initial scores is only influenced by measurement errors, the coefficient of regression \( b \) equals the final test score on the initial test score is only influenced by measurement errors, and the regression coefficient \( b \) will be close to \( r_{XY} \). Although the use of expression 3 is preferred for conceptual reasons, the outcomes of the various RCIs incorporating expressions 2, 3, or 4 as standard error will be similar.

When initial and final variance differ significantly, \( b \) and \( r_{XY} \) are notably different as well, and in addition to regression to the mean as a consequence of measurement errors, effects of testing are also present. When \( b > r_{XY} \), the final variance exceeds the initial variance, and when \( b < r_{XY} \), the final variance is smaller than the initial variance. In principle, method 2 should then be used, because the regression method uses the available information more thoroughly.

(c) However, because the coefficient of regression of the difference scores on the initial scores is equal to \( b-1 \), no useful information can be extracted from this regression when \( b \) is approximately 1. In that case, method 2 and method 1 incorporating expression 3 as standard error coincide—even the standard errors coincide—and method 1 incorporating expression 3 can be applied. When there is a significant practice effect in the control group does not significantly deviate from 0, the classic approach can be used—that is, the JT method with expression 3 as standard error.

From the foregoing outline, on the one hand, it can be concluded that method 1 using expression 3 in the denominator is a special case of method 2, which can be viewed as another argument that expression 3 is conceptually preferred. On the other hand, the classic approach using expression 3 is a special case of method 1 using expression 3. Thus, method 1 takes an intermediate position. Many researchers and clinicians will prefer to use this method, when the more elaborate method 2 is not indicated.

**COMPARING APPROACHES IN PRACTICE**

This discussion of the differences between the standard errors resulting from expressions 2, 3, and 4 will now be illustrated with an example from sport concussion research literature. For this example, outcomes are borrowed from the study by Iverson et al. This study involved five composites assessed in a control group where no intervention was conducted, including four scales measuring cognitive function (verbal memory, visual memory, reaction time, processing speed) and a postconcussion symptoms scale. Table 1 shows outcomes already presented by the authors, as well as additionally calculated outcomes (including the standard error according to expression 2 and regression coefficient \( b = r_{XY}S_Y/S_X \)).

At first glance, the table reveals that the standard error calculated according to expression 4 is indeed always larger than that calculated according to expression 3.

Considering the outcomes for the five tests successively, we see that verbal memory showed no notable increase in the group mean, but did show a notable diminution of the variance, which failed to be significant (\( t = 1.66, p=0.10 \)). As a consequence, the outcome of expression 2 was 8% larger than that of expression 3. The results for visual memory resembled the “ideal” outcomes described above and will not be discussed further. Reaction time showed a very small diminution of the group mean but a significant diminution of the variance (\( t = 3.94, p=0.001 \)), resulting in a large difference between the outcomes of expressions 2 and 3, the former being 14% larger, and the largest difference (10%)
observed between the outcomes of expressions 3 and 4. Procession speed showed a notable increase in the group mean, but no significant change in the variance ($t = 1.14, p=0.10$). Iverson et al. reported significant practice effects as shown by a paired samples $t$ test, which led the authors to apply method 1. Although not a cognitive measure, the results for the post concussion symptoms scale in the control group are also interesting. The mean showed a notable but not significant increase, while the increase in the variance was significant ($t = -2.26, p<0.05$), resulting in a 7% larger standard error according to expression 4 and a 21% smaller standard error according to expression 2, as compared with the outcome of expression 3. The value of the test-retest reliability is moderate and the regression coefficient is close to 1, suggesting that the regression to the mean as a consequence of measurement errors is overshadowed by a regression from the mean. The mechanism is not entirely clear, but it possibly evidences greater consciousness of complaints when the questionnaire is completed for a second time, which may be regarded as a specific type of practice effect.

Having applied the classic approach (or in particular method 1 incorporating expression 3 in the case of the processing speed test), Iverson et al. concluded that “the percentages of subjects that would be classified as reliably improved or declined was reasonably close to what would be predicted from the theoretical normal distribution”. However, the authors did not compare the results of applying the classic approach using expression 3 with those of other methods. In this respect, I wish to make several comments. Firstly, Temkin and colleagues, who used essentially the same approach as that proposed by Collie and colleagues, reported for the vast majority of the outcome measures included in their research results that did not evidence sufficient variability of the practice effects to yield notably different outcomes for expressions 3 and 4. A striking exception, however, was the trail making test. At the second assessment, this test showed a considerable decrease in the variance, suggesting that this measure was largely affected by variable practice effects. As a consequence, the standard error of the Temkin et al. approach was 23% larger than that according to expression 3. The Temkin et al. approach yielded a 90% confidence interval of width 0.83, cutting off only 5% of false positives (whereas 10% was expected on the basis of chance). The use of expression 3 yielded an interval of width 0.67 (number of false positives not reported), whereas the interval really delimiting the most extreme 10% of the participants was of width 0.48, as revealed by a distribution-free approach (table 6 of Temkin et al.). Thus, as the interval width yielded by expression 3 was far closer to reality, the results were clearly in favour of the classic approach using expression 3.

Secondly, I note that seemingly moderate differences between the sizes of the standard errors and between the numbers of false positives in the control sample may result in considerable differences between the percentages of patients submitted to an intervention, who are assessed as reliably changed.

Thirdly, in the Iverson et al. study, the regression method was not considered for application. However, for instance, for reaction time, the parameter estimations calculated in the control group possibly indicated the use of this method, which would lead to a standard error 20% smaller than expression 3. The difference between the resulting percentages of patients submitted to an intervention and assessed as reliably changed is probably spectacular.

**DISCUSSION**

This exposé has led to the conclusion that the standard error proposed by Collie et al. (expression 4) is always at least equal to or larger than the conceptually preferred expression 3. The distinction between the two standard errors is particularly relevant when the use of the Chelune et al. method is indicated. The circumstance that the Collie et al. method is more conservative implies that the probability of an unwarranted designation of reliable change is diminished. This may seem more preferable, but the tradeoff is a higher risk of not detecting real change. This tradeoff does not appear to be favourable to sport concussion diagnosis and management. On the one hand, a confidence interval that is too wide prevents a clinician from reliably concluding that the cognitive function of an athlete who has sustained a concussion has deteriorated. On the other hand, a too wide interval prevents a clinician from detecting subtle changes of

<table>
<thead>
<tr>
<th>Test</th>
<th>$M_x$</th>
<th>$M_y$</th>
<th>$M_y-M_x$</th>
<th>SDx</th>
<th>SDy</th>
<th>$r_{xy}$</th>
<th>$b_{yx}$</th>
<th>Expr 2</th>
<th>Expr 3</th>
<th>Expr 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Verbal memory</td>
<td>88.68</td>
<td>88.64</td>
<td>0.16</td>
<td>5.90</td>
<td>5.90</td>
<td>0.05</td>
<td>0.50</td>
<td>7.36</td>
<td>6.83</td>
<td>6.94</td>
</tr>
<tr>
<td>Visual memory</td>
<td>78.70</td>
<td>77.48</td>
<td>-1.22</td>
<td>13.39</td>
<td>13.39</td>
<td>0.67</td>
<td>0.67</td>
<td>10.88</td>
<td>10.59</td>
<td>10.61</td>
</tr>
<tr>
<td>Reaction time</td>
<td>0.543</td>
<td>0.536</td>
<td>0.007</td>
<td>0.07</td>
<td>0.07</td>
<td>0.063</td>
<td>0.57</td>
<td>0.056</td>
<td>0.049</td>
<td>0.054</td>
</tr>
<tr>
<td>Procession speed</td>
<td>40.54</td>
<td>42.24</td>
<td>1.70</td>
<td>7.64</td>
<td>7.64</td>
<td>0.068</td>
<td>0.79</td>
<td>4.04</td>
<td>3.89</td>
<td>3.93</td>
</tr>
<tr>
<td>PSS</td>
<td>5.23</td>
<td>5.79</td>
<td>0.56</td>
<td>6.75</td>
<td>6.75</td>
<td>1.00</td>
<td>0.65</td>
<td>5.65</td>
<td>7.17</td>
<td>7.66</td>
</tr>
</tbody>
</table>

Expr, Expression; PSS, post concusslon symptom scale.
cognitive function still present after a period of recovery, enhancing the conclusion that the cognitive function of this athlete has returned to baseline. Thus, if the method proposed by Collie and colleagues is used, there is a greater risk of an unwarranted return of an athlete to the arena after concussion. This risk is admittedly mitigated by the cautious way of using this method advocated by its authors (p 276).2

Within this context, it is clear that the suggestion of Collie et al.,3 adopted from Hinton-Bayre et al.,4 to assess healthy sportsmen twice with alternative test forms at the beginning of the season should be strongly endorsed, especially if methods are pursued that rule out practice effects. Such assessments will provide more accurate establishment of the test-retest reliability and thus of the reliability of change, which is important for methodical soundness and, of course, for the benefit of the sportsmen’s health.

As for methods for the assessment of reliable change, other than those compared in the present article, Collie and colleagues25 should be praised for their effort of bringing together current methods from various research areas. However, in my view, their review of these methods did not serve its audience well. The formulas covering the procedures that are in use in the fields with which I am familiar (psychotherapy and neuropsychology research) are highly idiosyncratic. To be honest, I do not understand the denotation of some of them, and I doubt that the readership of this journal does. Furthermore, Collie and colleagues25 cited one of my papers,4 which pointed out serious flaws of two of the methods most extensively cited by Collie et al.2,4 As for the method proposed by Zegers and Hafkenscheid,19 the latter authors themselves recognised the shortcomings of their proposal, which they no longer endorse.20 Apart from being based on the concept of Zegers and Hafkenscheid, the proposal of Bruggemans and associates21 bears a serious mistake and should also not be applied.8 Most surprisingly for the method proposed by Zegers and Hafkenscheid,19 the latter authors themselves recognised the shortcomings of their proposal, which they no longer endorse.20 Apart from being based on the concept of Zegers and Hafkenscheid, the proposal of Bruggemans and associates21 bears a serious mistake and should also not be applied.8 Most surprisingly to me, one of the methods listed24 was ascribed to me. However, I do not understand this method as denoted by Collie et al. I cannot even remember having proposed a new method in the paper cited. On the contrary, I have only attempted to demonstrate that the classic approach presented long ago by McNemar is undeservedly regarded as less dependable for a dependable assessment of change by authors who subsequently presented more sophisticated procedures for a reliable assessment of change.

Competing interests: none declared

REFERENCES
19 Hafkenscheid AJPM. De onverbeterlijke neiging tot ‘verbetering’ van veranderingscores: terug naar de aarzelijke index voor betrouwbaar verandering. (The incorrigible tendency to correct change scores: back to the original index for reliable change). Gedragstherapie 2002;35:317–27.

The debate over which approach to reliable change is most appropriate to determine significant change in an individual’s psychological test scores continues. In a series of papers, Maassen has argued that classical test theory has been unjustifiably ignored by many researchers in the area, and this most recent submission continues this idea. Maassen focuses on what he maintains is an erroneous suggestion of Collie and colleagues,3 where the latter authors appear to have unknowingly adopted an error term that was earlier proposed by Temkin and colleagues.18 The interested reader is directed to a series of papers appearing in the Journal of the International Neuropsychological Society (volume 10) which consider the issues in more detail (see Maassen3 and associated dialogues). Although Maassen’s discourse is instructive, it is unclear why the regression approach was not presented in more detail. Not only is it proposed by Maassen to be preferable under certain circumstances, but it has also been applied in sports concussion research.4,5 Using the data of Iverson and colleagues,6 it can be determined that the error terms for the McSweeney regression approach (standard error of prediction (SEP)) are smaller than any of the other options (expressions 2, 3, and 4) for all tests bar one, the post-concussion scale. This exception is notable as it suggests when the regression approach may be limited—as discussed below. The regression error values are: verbal memory SEP = 5.83, visual memory SEP = 9.51, reaction time SEP = 0.039, processing speed SEP = 3.64, and post-concussion scale SEP = 7.72.

It is my position that the regression approach to reliable change is preferable in most circumstances. I will elaborate on this further, but first to clarify how the RC methods can be practically compared. The RC approaches considered here can all take the general form of \( RC = (Y-Y^*)/SE \), where \( Y \) is the actual post score, \( Y^* \) the predicted post score, and SE a standard error. With a 90% level of confidence, any RC exceeding about 1.645 suggests significant individual change on retest. What varies from one approach to the next is the way in which \( Y \) and \( Y^* \) are derived. For the original
approach of Jacobson and Truax, $Y' = Y$, and $SE$ was originally based on expression 2 (in Maassen’s paper), with a recommendation to use expression 3 when posttest values are available, not expression 4. However, as Maassen notes, neuropsychological tests are often subjected to practice/learning effects, and thus this must be taken into account. In response to this problem, Chelune and colleagues calculated $Y'$ by adding the mean practice effect observed in a control population (or sample) to the pretest score. Maassen again advocates the use of expression 3 over both expressions 2 and 4. Note that the approach of Chelune et al adjusts “practice” identically for all individuals. Yet, whenever a measure is not perfectly reliable (practically always!), regression to the mean (RTM) will be present. This may be readily determined by obtaining a significant regression of difference scores ($Y-X$) on pretest scores ($X$).

The approach of McSweeny and colleagues adjusts for this, such that $Y'$ is estimated on the basis of the simple $Y' = bX + c = X$ for a linear prediction. With this approach, more extreme values at pretest are predicted to be closer to the mean on retest, thus each score is adjusted individually on the basis of relative position at pretest. The SEP is used as the mean on retest, thus each score is adjusted individually more extreme values at pretest are predicted to be closer to the mean, as indicated by the significantly larger regression to the mean (RTM) will be present. This may be readily determined by obtaining a significant regression of difference scores ($Y-X$) on pretest scores ($X$).

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